

# A Comparison of Color Difference Data and Formulas

BY

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$$L^* = L^*$$



$$B = B$$

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$$B = B$$



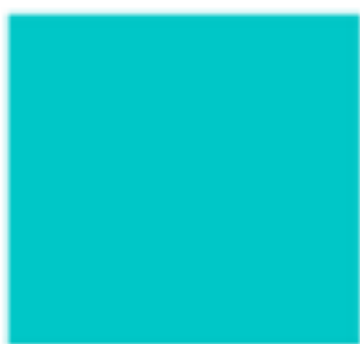












# IQ Colour – Color Space XYZ to Qtd

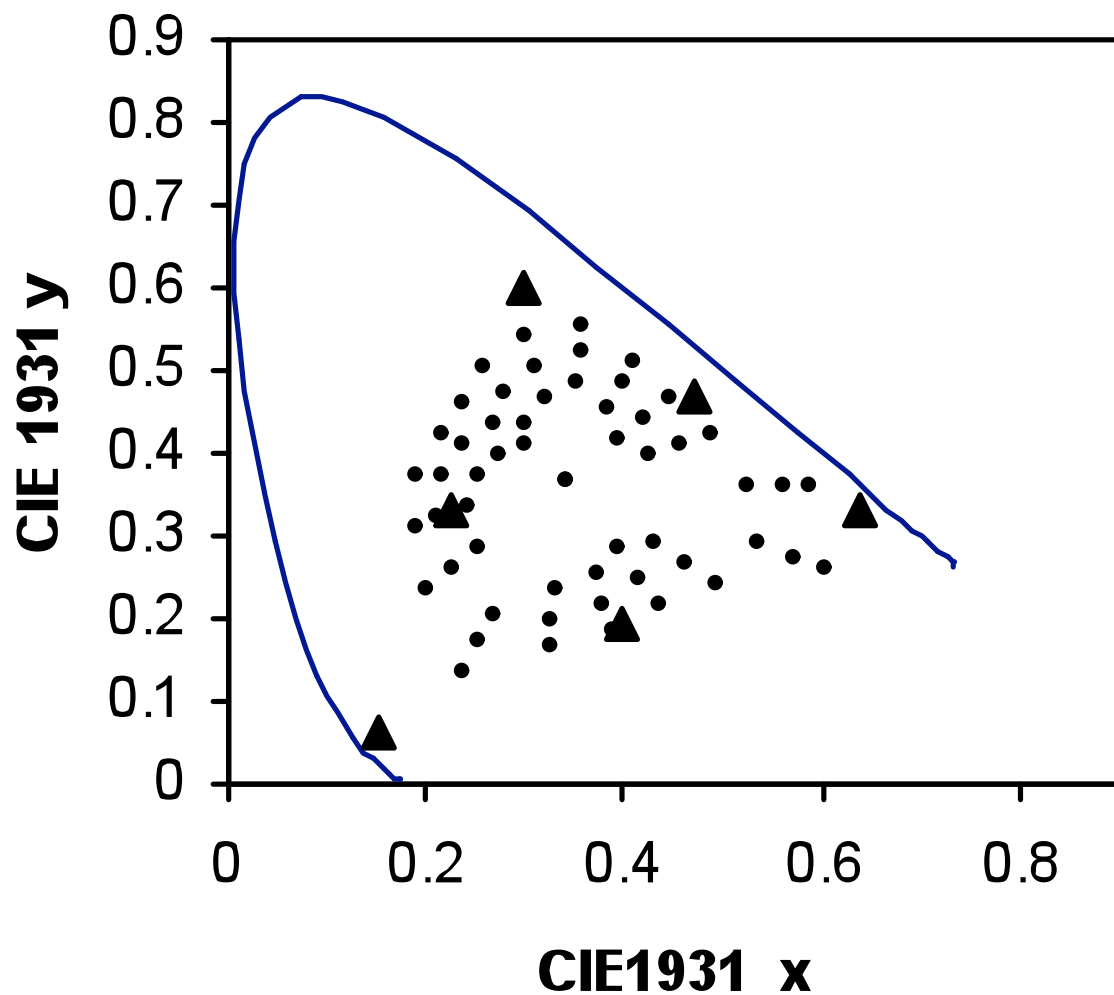
$$[ATD] = [LMS] * \begin{bmatrix} .6352 & .8057 & .3021 \\ .3915 & -1.084 & -.0931 \\ 0 & .2056 & -.3618 \end{bmatrix}$$

## IQ Colour – Perception Space

$$Q = A + T / 2 - D$$

$$t = T/Q \quad \text{and} \quad d = D/Q$$

# Brightness – Lightness Study



— Spectrum Locus

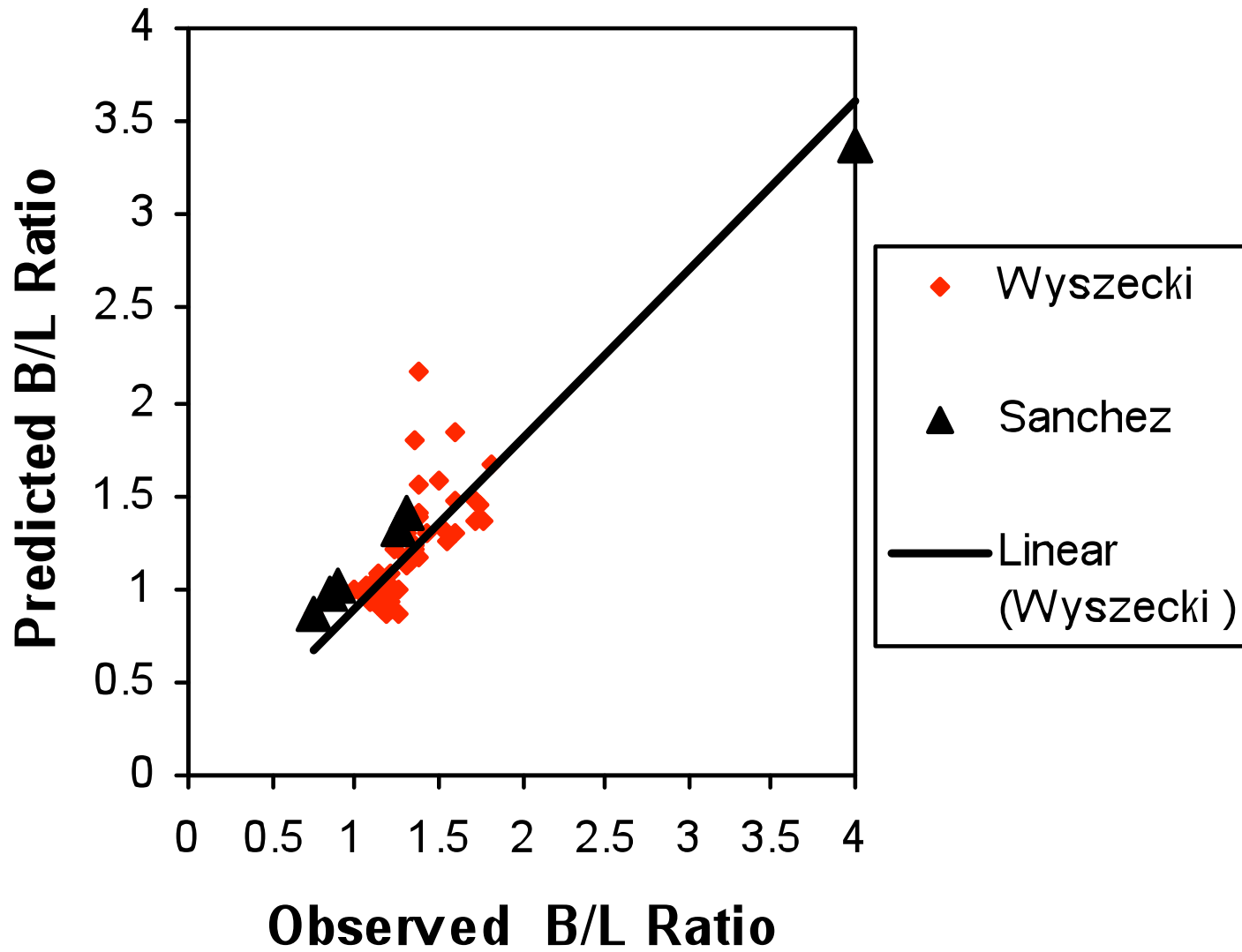
• Wyszecki & Stiles

▲ Sanchez & Fairchild

# Brightness Lightness Ratio

- The old ATD – Qtd Model used
  - $Q = A + T / 2 - D$
  - Did not take account of Blue – Yellow Interaction
  - Proposed
    - $Q = A + C1 * T + C2 * D$  for the Yellow Region
    - $Q = A + C1 * T + C3 * D$  for the Blue Region

# Brightness to Luminance Ratio



# Brightness Formula

$$Q = A + 0.5 * T \rightarrow \text{Yellow}$$

$$Q = A + 0.5 * T - 0.75 * D \rightarrow \text{Blue}$$

# Just Noticeable Difference Formula Development

- Test only JNDs less than 5
- Use Least Absolute Regression
- Visual Channels
  - Q, t and d
- Simple City Block Metric

# Delta Perception Model

- $S$  = absolute value of the greater of  $t$  or  $d$
- $H$  = absolute value of the lesser of  $t$  or  $d$
- $DP = a * |\Delta Q|^\gamma + b * |\Delta S|^\gamma + c * |\Delta H|^\gamma$

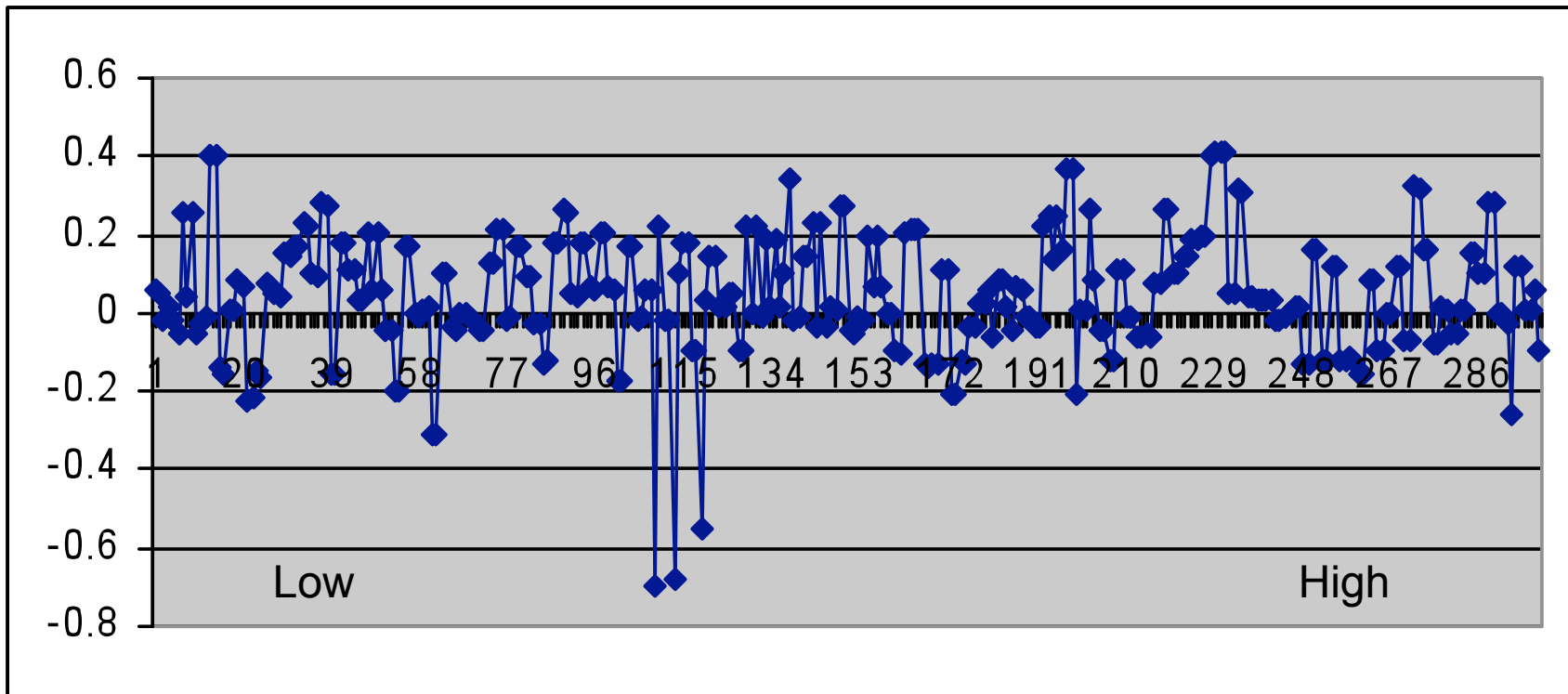


# Delta P Color Difference

$$DP = 1.9 * |\Delta Q|^{1/3} + 1.9 * |\Delta S|^{1/3} + 2.5 * |\Delta H|^{1/3}$$

# JND Error vs Luminance

## RIT-DuPont Data



# XYZ to Lab

$$\begin{aligned}x_r &= \frac{X}{X_r} & f_x &= \begin{cases} \sqrt[3]{x_r} & x_r > \varepsilon \\ \frac{\kappa x_r + 16}{116} & x_r \leq \varepsilon \end{cases} & L &= 116 f_y - 16 \\y_r &= \frac{Y}{Y_r} & f_y &= \begin{cases} \sqrt[3]{y_r} & y_r > \varepsilon \\ \frac{\kappa y_r + 16}{116} & y_r \leq \varepsilon \end{cases} & a &= 500(f_x - f_y) \\z_r &= \frac{Z}{Z_r} & f_z &= \begin{cases} \sqrt[3]{z_r} & z_r > \varepsilon \\ \frac{\kappa z_r + 16}{116} & z_r \leq \varepsilon \end{cases} & b &= 200(f_y - f_z)\end{aligned}$$

# Delta E CIE-76

$$\Delta E = \sqrt{(L_1 - L_2)^2 + (a_1 - a_2)^2 + (b_1 - b_2)^2}$$

# DE CIE(CMC)

$$\Delta C = C_1 - C_2$$

$$C_1 = \sqrt{a_1^2 + b_1^2}$$

$$C_2 = \sqrt{a_2^2 + b_2^2}$$

$$\Delta H = \sqrt{\Delta a^2 + \Delta b^2 - \Delta C^2}$$

$$\Delta L = L_1 - L_2$$

$$\Delta a = a_1 - a_2$$

$$\Delta b = b_1 - b_2$$

$$S_L = \begin{cases} 0.511 & L_1 < 16 \\ \frac{0.040975 L_1}{1 + 0.01765 L_1} & L_1 \geq 16 \end{cases}$$

$$S_C = \frac{0.0638 C_1}{1 + 0.0131 C_1} + 0.638$$

$$S_H = S_C (FT + 1 - F)$$

$$T = \begin{cases} 0.56 + |0.2 \cos(H_1 + 168)| & 164 \leq H_1 \leq 345 \\ 0.36 + |0.4 \cos(H_1 + 35)| & \text{otherwise} \end{cases}$$

$$F = \sqrt{C_1^4 / (C_1^4 + 1900)}$$

$$H_1 = \tan^{-1}(b_1/a_1)$$

$$\Delta E = \sqrt{(\Delta L/l S_L)^2 + (\Delta C/c S_C)^2 + (\Delta H/S_H)^2}$$

# Delta E CIE 94

$$\Delta L = L_1 - L_2$$

$$\Delta C = C_1 - C_2$$

$$\Delta H = \sqrt{\Delta a^2 + \Delta b^2 - \Delta C^2}$$

$$C_1 = \sqrt{a_1^2 + b_1^2}$$

$$C_2 = \sqrt{a_2^2 + b_2^2}$$

$$\Delta a = a_1 - a_2$$

$$\Delta b = b_1 - b_2$$

$$S_L = 1$$

$$S_C = 1 + K_1 C_1$$

$$\Delta E = \sqrt{\left(\frac{\Delta L}{K_L S_L}\right)^2 + \left(\frac{\Delta C}{K_C S_C}\right)^2 + \left(\frac{\Delta H}{K_H S_H}\right)^2}$$

# Delta E CIE2000

$$\bar{L}' = (L_1 + L_2)/2$$

$$C_1 = \sqrt{a_1^2 + b_1^2}$$

$$C_2 = \sqrt{a_2^2 + b_2^2}$$

$$\bar{C} = (C_1 + C_2)/2$$

$$G = \left(1 - \sqrt{\frac{\bar{C}^7}{\bar{C}^7 + 25^7}}\right) / 2$$

$$a'_1 = a_1(1+G)$$

$$a'_2 = a_2(1+G)$$

$$C'_1 = \sqrt{a'^2_1 + b_1^2}$$

$$C'_2 = \sqrt{a'^2_2 + b_2^2}$$

$$\bar{C}' = (C'_1 + C'_2)/2$$

$$h'_1 = \begin{cases} \tan^{-1}(b_1/a'_1) & \tan^{-1}(b_1/a'_1) \geq 0 \\ \tan^{-1}(b_1/a'_1) + 360^\circ & \tan^{-1}(b_1/a'_1) < 0 \end{cases}$$

$$h'_2 = \begin{cases} \tan^{-1}(b_2/a'_2) & \tan^{-1}(b_2/a'_2) \geq 0 \\ \tan^{-1}(b_2/a'_2) + 360^\circ & \tan^{-1}(b_2/a'_2) < 0 \end{cases}$$

$$\bar{H}' = \begin{cases} (h'_1 + h'_2 + 360^\circ)/2 & |h'_1 - h'_2| > 180^\circ \\ (h'_1 + h'_2)/2 & |h'_1 - h'_2| \leq 180^\circ \end{cases}$$

$$T = 1 - 0.17 \cos(\bar{H}' - 30^\circ) + 0.24 \cos(2\bar{H}') + 0.32 \cos(3\bar{H}' + 6^\circ) - 0.20c$$

$$\Delta h' = \begin{cases} h'_2 - h'_1 & |h'_2 - h'_1| \leq 180^\circ \\ h'_2 - h'_1 + 360^\circ & |h'_2 - h'_1| > 180^\circ; h'_2 \leq h'_1 \\ h'_2 - h'_1 - 360^\circ & |h'_2 - h'_1| > 180^\circ; h'_2 > h'_1 \end{cases}$$

$$\Delta E = \sqrt{\left(\frac{\Delta L'}{K_L S_L}\right)^2 + \left(\frac{\Delta C'}{K_C S_C}\right)^2 + \left(\frac{\Delta H'}{K_H S_H}\right)^2 + R_T \left(\frac{\Delta C'}{K_C S_C}\right) \left(\frac{\Delta H'}{K_H S_H}\right)}$$

# IQ Colour – Color Space

## XYZ to Qtd

$$[ATD] = [LMS] * \begin{bmatrix} .6352 & .8057 & .3021 \\ .3915 & -1.084 & -.0931 \\ 0 & .2056 & -.3618 \end{bmatrix}$$

## IQ Colour – Perception Space

$$Q = A + T / 2 - D$$

$$t = T/Q \quad \text{and} \quad d = D/Q$$



# Delta Perception

S = absolute value of the greater of t or d

H= absolute value of the lesser of t or d

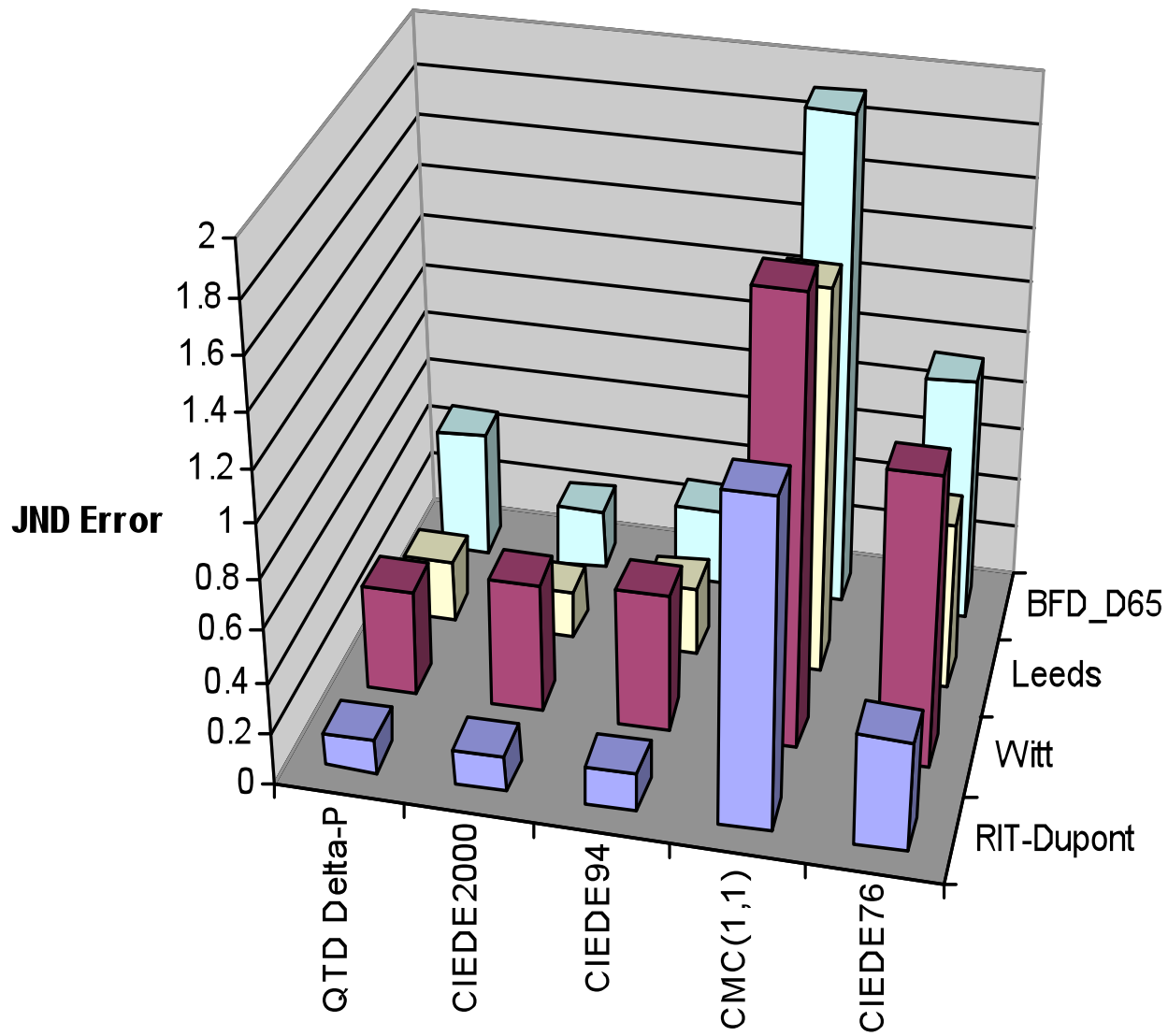
R= H / S

$$DP = 1.9 * |\Delta Q|^{1/3} + 1.9 * |\Delta S|^{1/3} + 2.5 * |\Delta H|^{1/3}$$

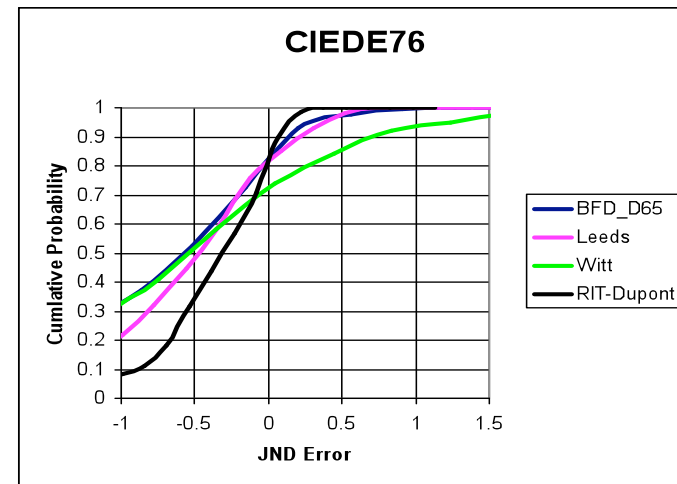
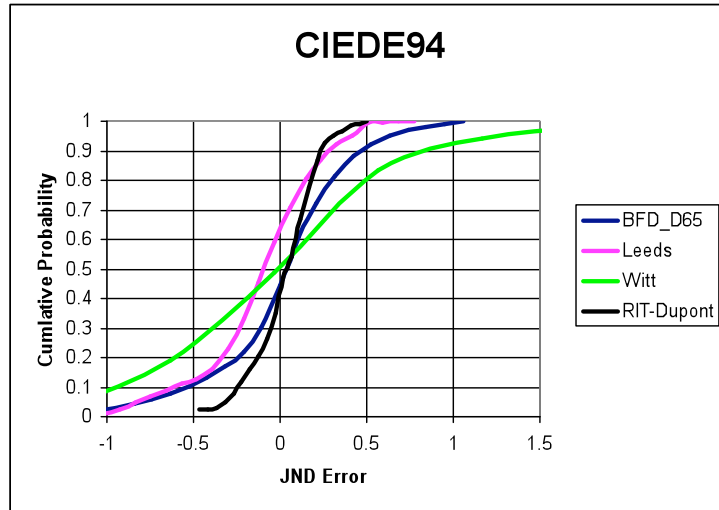
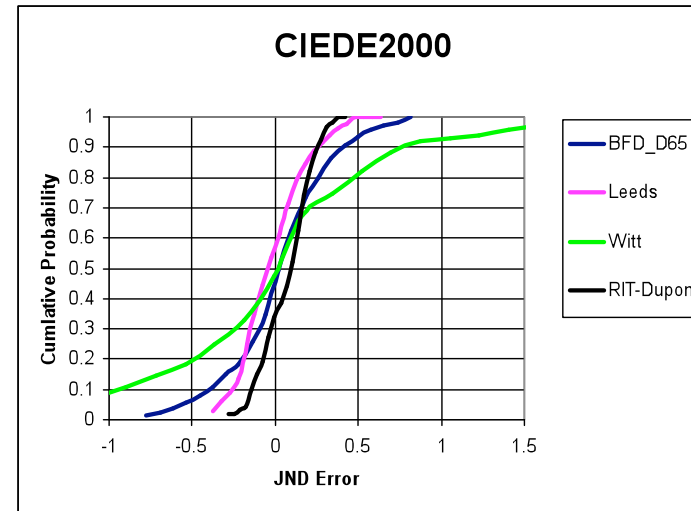
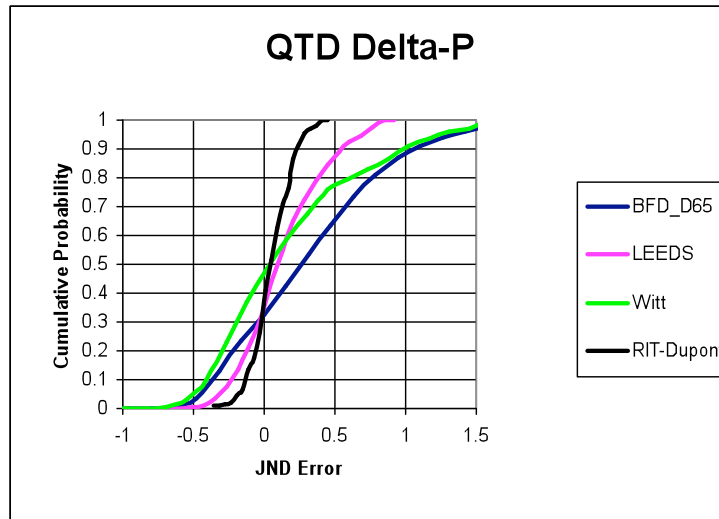
# Least Absolute Error

	<b>QTD Delta-P</b>	<b>CIEDE2000</b>	<b>CIEDE94</b>	<b>CMC(1,1)</b>	<b>CIEDE76</b>
<b>RIT-Dupont</b>	<b>0.12</b>	<b>0.14</b>	<b>0.15</b>	<b>1.25</b>	<b>0.42</b>
<b>Witt</b>	<b>0.41</b>	<b>0.50</b>	<b>0.53</b>	<b>1.72</b>	<b>1.11</b>
<b>Leeds</b>	<b>0.24</b>	<b>0.18</b>	<b>0.27</b>	<b>1.50</b>	<b>0.66</b>
<b>BFD_D65</b>	<b>0.49</b>	<b>0.24</b>	<b>0.30</b>	<b>1.92</b>	<b>0.95</b>

# Absolute Error Summary



# Statistical DE Comparison



# Conclusions

- A simple vision based non-Euclidean Model
  - Performs as well as the more complex CIE color difference formulas.
- The noise in the measured data was equal to the prediction error of DP.
- The data set used to develop CIE DE2000 is in question as to its validity.
- CIE DE2000 is equivalent to CIE DE94

QUESTIONS ?